

UČNI NAČRT PREDMETA / COURSE SYLLABUS						
<b>Predmet:</b>		Diferencialna geometrija				
<b>Course title:</b>		Differential geometry				
<b>Študijski program in stopnja</b> Study programme and level		<b>Študijska smer</b> Study field		<b>Letnik</b> Academic year	<b>Semester</b> Semester	
Magistrski študijski program Finančna matematika		ni smeri		1 ali 2	prvi ali drugi	
Master's study programme Financial Mathematics		none		1 or 2	first or second	
<b>Vrsta predmeta / Course type</b>				izbirni		
<b>Univerzitetna koda predmeta / University course code:</b>				M2315		
<b>Predavanja</b> Lectures	<b>Seminar</b> Seminar	<b>Vaje</b> Tutorial	<b>Klinične vaje</b> work	<b>Druge oblike študija</b>	<b>Samost. delo</b> Individ. work	<b>ECTS</b>
45		30			105	6
<b>Nosilec predmeta / Lecturer:</b>		prof. Janez Mrčun, prof. Pavle Saksida, prof. Sašo Strle				
<b>Jeziki / Languages:</b>		<b>Predavanja / Lectures:</b> slovenski/Slovene, angleški/English				
		<b>Vaje / Tutorial:</b> slovenski/Slovene, angleški/English				
<b>Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:</b>				<b>Prerequisites:</b>		
<b>Vsebina:</b>				<b>Content (Syllabus outline):</b>		
Obvezni del:  Uvod in osnovni pojmi: Vektorska polja in Liejev oklepaj. Temeljni pojmi teorije Liejevih				Core topics:  Introduction: Vector fields and Lie bracket. Fundamental notions of the Lie theory. Differential forms. Vector bundles, Riemann		

<p>grup in Liejevih algeber. Diferencialne forme. Vektorski svežnji in Riemannove strukture na njih.</p> <p>Glavni svežnji, pridruženi svežnji, sveženj ogrodij, pojem redukcije svežnja.</p> <p>Diferencialne forme z vrednostmi v Liejevih algebrah, povezave na glavnem svežnju. Horizontalni dvig poti. Ukrivljenost in holonomija. Različni opisi ukrivljenosti na glavnem svežnju.</p> <p>Povezave na vektorskih svežnjih, kovariantni odvod. Chernovi razredi.</p> <p>Temelji Riemannove geometrije: Riemannova metrika, Levi-Civitéjeva povezava, Riemannov tenzor ukrivljenosti in njegove lastnosti, Riccijeva in Weylova ukrivljenost, avtoparalelnost, geodetske krivulje. Eksponentna preslikava.</p> <p>Izbirni del:</p> <p>Podgrupe grupe <math>GL(n, \mathbb{C})</math> in simetrični prostori. Gaussova ukrivljenost na ploskvah. Poissonove in simplektične mnogoterosti. Pontrjaginski razredi in Bottov izrek. Konformnost in Weylov tenzor.</p>	<p>structures on vector bundles.</p> <p>Principal bundles, associated bundles, frame bundles, reductions of bundles.</p> <p>Differential forms with values in Lie algebras, connections on principal bundles. Horizontal lift of a path. Curvature and holonomy. Various descriptions of the curvature on a principal bundle.</p> <p>Connections on vector bundles, covariant derivative. Chern classes.</p> <p>Fundamental notions of Riemann geometry: Riemannian metric, Levi-Civité connection, Riemann curvature tensor and its properties, Ricci and Weyl curvatures, autoparallel curves, geodesic curves. Exponential map.</p> <p>Additional topics: Subgroups of the group <math>GL(n, \mathbb{C})</math> and symmetric spaces. Gaussian curvature on surfaces. Poisson and symplectic manifolds. Pontryagin classes and Bott's theorem. Conformality and Weyl tensor</p>
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### Temeljni literatura in viri / Readings:

B. A. Dubrovin, A. T. Fomenko, S. P. Novikov: Modern Geometry - Methods and Applications II : The Geometry and Topology of Manifolds, Springer, New York, 1985.

S. Helgason: Differential Geometry, Lie Groups, and Symmetric Spaces, AMS, Providence, 2001.

S. Kobayashi, K. Nomizu: Foundations of Differential Geometry I, II, John Wiley & Sons, New York, 1996.

P. Petersen: Riemannian Geometry, Springer, New York, 1997.

J. Cheeger, D. Ebin, Comparison Theorems in Riemannian Geometry, AMS Chelsea Publishing, Providence, 2008

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**Cilji in kompetence:**

Študent se spozna s temelji sodobne diferencialne geometrije. Osnovna pojma tega predmeta sta povezava na glavnem ali na vektorskem svežnju in ukrivljenost povezave. Ukrivljenost je predstavljena skozi optiko Frobeniusovega izreka. Vpeljan je pojem holonomije, opisana je zveza med ukrivljenostjo in holonomijo. Te pojme uporabimo pri obravnavi temeljev Riemannove geometrije. Prek Chernovih razredov poudarimo povezavo s topologijo.

**Objectives and competences:**

Fundamental concepts of modern differential geometry are introduced. The central objects of the course are connections on principal or vector bundles and their curvatures. The curvature is described from the point of view of the Frobenius theorem. The notion of holonomy is introduced and the relationship between holonomy and curvature is described. These notions are then used in the presentation of the fundamentals of the Riemannian geometry. The relationship between differential geometry and topology is illustrated by means of Chern classes.

**Predvideni študijski rezultati:**

Znanje in razumevanje: Poznavanje in razumevanje osnovnih pojmov in definicij iz diferencialne geometrije.  
Uporaba: Uporaba teorije pri reševanju problemov.

Refleksija: Razumevanje teorije na podlagi uporabe.

Prenosljive spretnosti – niso vezane le na en predmet: Spretnosti uporabe domače in tuje literature in drugih virov, identifikacija in reševanje problemov, kritična analiza.

**Intended learning outcomes:**

Knowledge and understanding: Understanding the fundamental definitions and concepts of differential geometry.

Application: Solving problems by applying the relevant theory.

Reflection: Understanding the theory through its applications.

Transferable skills: Skills in the use of the relevant literature and other sources, formulating problems and solving them, critical analysis.

**Metode poučevanja in učenja:**

predavanja, vaje, domače naloge, konzultacije

**Learning and teaching methods:**

Lectures, exercises, homework, consultations

<b>Načini ocenjevanja:</b>	<b>Weight (in %)</b>	<b>Assessment:</b>
pisni izpit ustni izpit		written exam oral exam
Ocene: 1-5 (negativno), 6-10 (pozitivno) (po Statutu UL)	50% 50%	Grading: 1-5 (fail), 6-10 (pass) (according to the Statute of UL)

#### **Reference nosilca / Lecturer's references:**

Janez Mrčun:

- MRČUN, Janez. An extension of the Reeb stability theorem. *Topology and its Applications*, ISSN 0166-8641. [Print ed.], 1996, let. 70, št. 1, str. 25-55 [COBISS.SI-ID 7630169]
- MOERDIJK, Ieke, MRČUN, Janez. On integrability of infinitesimal actions. *American journal of mathematics*, ISSN 0002-9327, 2002, vol. 124, no. 3, str. 567-593 [COBISS.SI-ID 11700057]
- MOERDIJK, Ieke, MRČUN, Janez. *Introduction to foliations and Lie groupoids*, (Cambridge studies in advanced mathematics, 91). Cambridge, UK: Cambridge University Press, 2003. IX, 173 str., ilustr. ISBN 0-521-83197-0 [COBISS.SI-ID 12683097]

Pavle Saksida:

- SAKSIDA, Pavle. Nahm's equations and generalizations Neumann system. *Proceedings of the London Mathematical Society*, ISSN 0024-6115, 1999, let. 78, št. 3, str. 701-720 [COBISS.SI-ID 8853849]
- SAKSIDA, Pavle. Integrable anharmonic oscillators on spheres and hyperbolic spaces. *Nonlinearity*, ISSN 0951-7715, 2001, vol. 14, no. 5, str. 977-994 [COBISS.SI-ID 10942809]
- SAKSIDA, Pavle. Lattices of Neumann oscillators and Maxwell-Bloch equations. *Nonlinearity*, ISSN 0951-7715, 2006, vol. 19, no. 3, str. 747-768 [COBISS.SI-ID 13932377]

Sašo Strle:

- STEFANOVSKA, Aneta, STRLE, Sašo, KROŠELJ, Peter. On the overestimation of the correlation dimension. *Physics letters. Section A*, ISSN 0375-9601. [Print ed.], 1997, vol. 235, str. 24-30 [COBISS.SI-ID 607828]
- RUBERMAN, Daniel, STRLE, Sašo. Mod 2 Seiberg-Witten invariants of homology tori. *Mathematical research letters*, ISSN 1073-2780, 2000, vol. 7, no. 5-6, str. 789-799 [COBISS.SI-ID 10557785]
- STRLE, Sašo. Bounds on genus and geometric intersections from cylindrical end moduli spaces. *Journal of differential geometry*, ISSN 0022-040X, 2003, vol. 65, no. 3, str. 469-511 [COBISS.SI-ID 13135193]

