

UČNI NAČRT PREDMETA / COURSE SYLLABUS (leto / year 2017/18)						
Predmet:		Uvod v funkcionalno analizo				
Course title:		Introduction to functional analysis				
Študijski program in stopnja Study programme and level		Študijska smer Study field		Letnik Academic year	Semester Semester	
Magistrski študijski program Matematika		ni smeri		1 ali 2	prvi ali drugi	
Master's study programme Mathematics		none		1 or 2	first or second	
Vrsta predmeta / Course type				izbirni temeljni / core elective		
Univerzitetna koda predmeta / University course code:				M2111		
Predavanja Lectures	Seminar Seminar	Vaje Tutorial	Klinične vaje work	Druge oblike študija	Samost. delo Individ. work	ECTS
45		30			105	6
Nosilec predmeta / Lecturer:		prof. dr. Roman Drnovšek, prof. dr. Bojan Magajna, prof. dr. Peter Šemrl				
Jeziki / Languages:		Predavanja / Lectures: slovenski / Slovene, angleški / English				
		Vaje / Tutorial: slovenski / Slovene, angleški / English				
Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:				Prerequisites:		
Vpis v letnik študija.				Enrolment in the programme.		
Vsebina:				Content (Syllabus outline):		

<p>Hilbertovi prostori. Ortonormirani sistemi. Besslova neenakost. Kompletnost. Fouriereve vrste. Parsevalova enakost.</p> <p>Linearni operatorji in funkcionali na Hilbertovih prostorih.</p> <p>Reprezentacija zveznega linearnega funkcionala.</p> <p>Adjungirani operator. Sebiadjungirani in normalni operatorji.</p> <p>Projektorji in idempotenti. Invariantni podprostor.</p> <p>Kompaktni operatorji. Spekter kompaktne operatorja.</p> <p>Diagonalizacija kompaktne sebiadjungiranega operatorja.</p> <p>Uporaba: Sturm-Liouillovi sistemi.</p> <p>Banachovi prostori. Primeri.</p> <p>Linearni operatorji in funkcionali na Banachovih prostorih.</p> <p>Končnorazsežni normirani prostori. Kvocienti in produkti normiranih prostorov.</p> <p>Hahn-Banachov izrek in posledice. Separacija konveksnih množic.</p>	<p>Hilbert spaces. Orthonormal systems. Bessel's inequality. Completeness. Fourier series. Parseval's identity.</p> <p>Linear operators and functionals on Hilbert spaces. The representation of a continuous linear functional. Adjoint operator. Selfadjoint and normal operators. Projectors and idempotents. Invariant subspaces. Compact operators. The spectrum of a compact operator. Diagonalization of a selfadjoint compact operator. An application: Sturm-Liouville systems. Banach spaces. Examples. Linear operators and functionals on Banach spaces. Finite dimensional normed spaces. Quotients and products of normed spaces. The Hahn-Banach theorem and consequences. Separation of convex sets.</p>
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Temeljni literatura in viri / Readings:

B. Bollobás: Linear Analysis : An Introductory Course, 2nd edition, Cambridge Univ. Press, Cambridge, 1999.

J. B. Conway: A Course in Functional Analysis, 2nd edition, Springer, New York, 1990.

Y. Eidelman, V. Milman, A. Tzolomitis: Functional Analysis : An Introduction, AMS, Providence, 2004.

D. H. Griffel: Applied Functional Analysis, Dover Publications, Mineola, 2002.

M. Hladnik: Naloge in primeri iz funkcionalne analize in teorije mere, DMFA-založništvo, Ljubljana, 1985.

E. Zeidler: Applied Functional Analysis : Main Principles and Their Applications, Springer, New York, 1995.

Cilji in kompetence:

Študent spozna osnovne pojme teorije Hilbertovih prostorov in linearnih operatorjev med njimi. Z njeno uporabo se seznanijo pri reševanju Sturm-Liouville problema. Nekoliko spozna tudi teorijo Banachovih prostorov, ki so posplošitev Hilbertovih prostorov.

Objectives and competences:

Students acquire basic knowledge of the theory of Hilbert spaces and linear operators between them. The theory is applied for solving simple Sturm-Liouville problems. Students also learn some basic concepts from the theory of Banach spaces, which are a generalization of Hilbert spaces.

Predvideni študijski rezultati:

Znanje in razumevanje: Razumevanje teorije Hilbertovih prostorov s teoretičnega in uporabnega vidika.
Uporaba: Uporaba funkcionalne analize sega tudi v naravoslovje in druga področja znanosti kot na primer ekonomijo.
Refleksija: Razumevanje teorije na podlagi uporabe.
Prenosljive spretnosti – niso vezane le na en predmet: Sposobnost abstraktnega razmišljanja. Spretnost uporabe domače in tuje literature.

Intended learning outcomes:

Knowledge and understanding: Understanding of the theory of Hilbert spaces.
Application: Functional analysis is used in natural sciences and other areas of science such as economics.
Reflection: Understanding of the theory on the basis of examples.
Transferable skills: Ability to use abstract methods to solve problems. Ability to use a wide range of references and critical thinking.

Metode poučevanja in učenja:

Learning and teaching methods:

predavanja, vaje, domače naloge, konzultacije	Lectures, exercises, homeworks, consultations
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		Delež (v %) / Weight (in %)	Assessment:
Načini ocenjevanja:			
Način (pisni izpit, ustno izpraševanje, naloge, projekt):			Type (examination, oral, coursework, project):
domače naloge			homeworks
izpit iz vaj	10%		written exam
ustni izpit	50%		oral exam
Ocene: 1-5 (negativno), 6-10 (pozitivno) (po Statutu UL)	40%		Grading: 1-5 (fail), 6-10 (pass) (according to the Statute of UL)

Reference nosilca / Lecturer's references:

Roman Drnovšek:

DRNOVŠEK, Roman. An irreducible semigroup of idempotents. *Studia Mathematica*, ISSN 0039-3223, 1997, let. 125, št. 1, str. 97-99. [COBISS.SI-ID 7436633]

DRNOVŠEK, Roman. Common invariant subspaces for collections of operators. *Integral equations and operator theory*, ISSN 0378-620X, 2001, vol. 39, no. 3, str. 253-266. [COBISS.SI-ID 10597721]

DRNOVŠEK, Roman. Invariant subspaces for operator semigroups with commutators of rank at most one. *Journal of functional analysis*, ISSN 0022-1236, 2009, vol. 256, iss. 12, str. 4187-4196. [COBISS.SI-ID 15167321]

Bojan Magajna:

MAGAJNA, Bojan. On tensor products of operator modules. *Journal of operator theory*, ISSN 0379-4024, 2005, vol. 54, no. 2, str. 317-337. [COBISS.SI-ID 13920089]

MAGAJNA, Bojan. Duality and normal parts of operator modules. *Journal of functional analysis*, ISSN 0022-1236, 2005, vol. 219, no. 2, str. 306-339. [COBISS.SI-ID 13366105]

MAGAJNA, Bojan. On completely bounded bimodule maps over W^* -algebras. *Studia*

Mathematica, ISSN 0039-3223, 2003, t. 154, fasc. 2, str. 137-164. [COBISS.SI-ID 12278105]

Peter Šemrl:

ŠEMRL, Peter, VÄISÄLÄ, Jussi. Nonsurjective nearisometries of Banach spaces. Journal of functional analysis, ISSN 0022-1236, 2003, vol. 198, no. 1, str. 268-278. [COBISS.SI-ID 12371545]

ŠEMRL, Peter. Generalized symmetry transformations on quaternionic indefinite inner product spaces: an extension of quaternionic version of Wigner's theorem. Communications in Mathematical Physics, ISSN 0010-3616, 2003, vol. 242, no. 3, str. 579-584. [COBISS.SI-ID 12770649]

ŠEMRL, Peter. Applying projective geometry to transformations on rank one idempotents. Journal of functional analysis, ISSN 0022-1236, 2004, vol. 210, no. , str. 248-257. [COBISS.SI-ID 13012825]