

UČNI NAČRT PREDMETA / COURSE SYLLABUS									
Predmet:	Uvod v algebraično geometrijo								
Course title:	Introduction to algebraic geometry								
Študijski program in stopnja Study programme and level	Študijska smer Study field		Letnik Academic year	Semester Semester					
Magistrski študijski program Matematika	ni smeri		1 ali 2	prvi ali drugi					
Master's study programme Mathematics	none		1 or 2	first or second					
Vrsta predmeta / Course type	izbirni								
Univerzitetna koda predmeta / University course code:	M2310								
Predavanja Lectures	Seminar Seminar	Vaje Tutorial	Klinične vaje work	Druge oblike študija	Samost. delo Individ. work	ECTS			
45		30			105	6			
Nosilec predmeta / Lecturer:	prof. Tomaž Košir								
Jeziki / Languages:	Predavanja / slovenski/Slovene, angleški/English Lectures:								
	Vaje / Tutorial: slovenski/Slovene, angleški/English								
Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:	Prerequisites:								
Vsebina:	Content (Syllabus outline):								
Osnovni del:  Afine raznoterosti. Hilbertov izrek o ničlah. Kolobar polinomskih funkcij. Racionalne	Fundamental part:  Affine varieties. Hilbert Nullstellensatz.  Ring of polynomial functions. Rational functions.								

funkcije.	Local properties of plane curves.
Lokalne lastnosti ravninskih krivulj.	Projective varieties. Regular and rational functions.
Projektivne raznoterosti. Regularne in racionalne funkcije.	Projective plane curves. Bezout's Theorem.
Projektivne ravninske krivulje. Bezoutev izrek. Izrek Maxa Noetherja.	Max Noether Theorem.
Preslikave med raznoterostmi. Resolucije singularnosti krivulj.	Affine and rational maps. Resolutions of singularities.
Hilbertov polinom in Hilbertova funkcija.	Hilbert polynomial and Hilbert function.
Delitelji na raznoterostih.	Divisors on varieties.
Krivulje. Ravninske kubične krivulje. Linearni sistemi na krivulji. Projektivne vložitve krivulj.	Curves. Plane cubic curves. Linear systems on curves. Projective embeddings of curves.
Izbirne vsebine:	Elective topics:
Riemann-Rochov izrek.	Riemann-Roch Theorem.

#### **Temeljni literatura in viri / Readings:**

- B. Hassett. Introduction to algebraic geometry. Cambridge Univ. Press, 2007.
- M. C. Beltrametti, E. Carletti, D. Gallarati, G. Monti Bragadin. Lectures on Curves, Surfaces and Projective Varieties. A Classical View of Algebraic Geometry, EMS Text-books in Mathematics, 2009.
- I. Shafarevich: Basic Algebraic Geometry I : Varieties in Projective Space, 2nd edition, Springer, Berlin, 1994.
- K. Hulek: Elementary Algebraic Geometry, AMS, Providence, 2003.
- W. Fulton: Algebraic Curves, Addison-Wesley, Redwood City, 1989.
- J. Harris: Algebraic Geometry : A First Course, Springer, New York, 1995.

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**Cilji in kompetence:**

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**Objectives and competences:**

Študent se spozna z osnovnimi pojmi in izreki algebraične geometrije.

Student masters basic concepts and tools of algebraic geometry.

**Predvideni študijski rezultati:**

Znanje in razumevanje: Poznavanje pojmov in izrekov algebraične geometrije in njihovo prepoznavanje v drugih vejah matematike.  
Uporaba: V področjih matematike, ki delajo z geometričnimi objekti, v teoretični fiziki, in druge.

Refleksija: Razumevanje teorije na podlagi primerov in uporabe.

Prenosljive spretnosti – niso vezane le na en predmet: Formulacija problemov v primernem jeziku, reševanje in analiza dobljenih rezultatov na primerih, prepoznavanje algebraičnih struktur v geometriji.

**Intended learning outcomes:**

Knowledge and understanding: Understanding of basic concepts and theorems of algebraic geometry, and their role in some other areas.  
Application: In the areas of mathematics that deal with geometric objects, in theoretical physics, and elsewhere.

Reflection: Understanding the theory on the basis of examples and applications.

Transferable skills: Formulation and solution of problems in an appropriate setup, solution and analysis of the results in examples, recognizing algebraic structures in geometric objects.

**Metode poučevanja in učenja:**

predavanja, vaje, domače naloge, konzultacije

**Learning and teaching methods:**

Lectures, exercises, homeworks, consultations

**Načini ocenjevanja:**

Način (pisni izpit, ustno izpraševanje, naloge, projekt):  
izpit iz vaj (2 kolokvija ali pisni izpit)

Delež (v %) /

Weight (in %)

**Assessment:**

50%  
50%

Type (examination, oral, coursework, project):  
2 midterm exams instead of written exam, written exam

ustni izpit		oral exam
Ocene: 1-5 (negativno), 6-10 (pozitivno) (po Statutu UL)		Grading: 1-5 (fail), 6-10 (pass) (according to the Statute of UL)

**Reference nosilca / Lecturer's references:**

Tomaž Košir:

- GRUNENFELDER, Luzius, KOŠIR, Tomaž. Geometric aspect of multiparameter spectral theory. *Transactions of the American Mathematical Society*, ISSN 0002-9947, 1998, let. 350, št. 6, str. 2525-2546 [COBISS.SI-ID 8449113]
- KOŠIR, Tomaž, SETHURAMAN, B. A. Determinantal varieties over truncated polynomial rings. *Journal of Pure and Applied Algebra*, ISSN 0022-4049. [Print ed.], 2005, vol. 195, no. 1, str. 75-95 [COBISS.SI-ID 13266265]
- BUCKLEY, Anita, KOŠIR, Tomaž. Plane curves as Pfaffians. *Annali della Scuola normale superiore di Pisa, Classe di scienze*, ISSN 0391-173X, 2011, vol. 10, iss. 2, str. 363-388 [COBISS.SI-ID 15928409]