

UČNI NAČRT PREDMETA / COURSE SYLLABUS						
Predmet:		Funkcionalna analiza				
Course title:		Functional analysis				
Študijski program in stopnja Study programme and level		Študijska smer Study field		Letnik Academic year		Semester Semester
Magistrski študijski program Matematika		ni smeri		1 ali 2		prvi ali drugi
Master's study programme Mathematics		none		1 or 2		first or second
Vrsta predmeta / Course type				izbirni		
Univerzitetna koda predmeta / University course code:				M2116		
Predavanja Lectures	Seminar Seminar	Vaje Tutorial	Klinične vaje work	Druge oblike študija	Samost. delo Individ. work	ECTS
45		30			105	6
Nosilec predmeta / Lecturer:		prof. Peter Šemrl, prof. Roman Drnovšek				
Jeziki / Languages:		Predavanja / Lectures: slovenski/Slovene, angleški/English				
		Vaje / Tutorial: slovenski/Slovene, angleški/English				
Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:				Prerequisites:		
Vsebina:				Content (Syllabus outline):		

<p>Banachovi prostori. Linearni operatorji in funkcionali na Banachovih prostorih.</p> <p>Izrek o odprti preslikavi. Izrek o zaprtem grafu. Princip enakomerne omejenosti. Drugi dual.</p> <p>Adjungirani operator na Banachovem prostoru.</p> <p>Šibke topologije. Banach-Alaoglujev izrek.</p> <p>Krein-Milmanov izrek o ekstremnih točkah.</p> <p>Banachove algebre. Ideali in kvocienti. Spekter elementa. Rieszov funkcijski račun. Gelfandova transformacija.</p> <p>C*-algebre. Približne enote. Ideali in kvocienti. Komutativne C*-algebre. Funkcijski račun v C*-algebrah. Gelfand-Naimark-Segalova konstrukcija.</p>	<p>Banach spaces. Linear operators and functionals on Banach spaces. The open mapping theorem. The closed graph theorem. The principle of uniform boundedness. The second dual. The adjoint operator on a Banach space. Weak topologies. The Banach-Alaoglu theorem. The Krein-Milman theorem on extreme points. Banach algebras. Ideals and quotients. The spectrum of an element. Riesz functional calculus. The Gelfand transform. C*-algebras. Approximate units. Ideals and quotients. Commutative C*-algebras. The functional calculus in C*-algebras. The Gelfand-Naimark-Segal construction.</p>
---	--

Temeljni literatura in viri / Readings:

B. Bollobás: Linear Analysis : An Introductory Course, 2nd edition, Cambridge Univ. Press, Cambridge, 1999.

J. B. Conway: A Course in Functional Analysis, 2nd edition, Springer, New York, 1990.

Y. Eidelman, V. Milman, A. Tzolomitis: Functional Analysis : An Introduction, AMS, Providence, 2004.

M. Hladnik: Naloge in primeri iz funkcionalne analize in teorije mere, DMFA-založništvo, Ljubljana, 1985.

R. Meise, D. Vogt: Introduction to Functional Analysis, Oxford Univ. Press, Oxford, 1997.

G. K. Pedersen: Analysis Now, Springer, New York, 1996.

W. Rudin: Functional Analysis, 2nd edition, McGraw-Hill, New York, 1991.

I. Vidav: Linearni operatorji v Banachovih prostorih, DMFA-založništvo, Ljubljana, 1982.

- I. Vidav: Banachove algebre, DMFA-založništvo, Ljubljana, 1982.

I. Vidav: Uvod v teorijo C*-algeber, DMFA-založništvo, Ljubljana, 1982.

Cilji in kompetence:

Slušatelj spozna osnove funkcionalne analize in povezavo z drugimi področji analize.

Objectives and competences:

Students learn the basics of functional analysis and links with other areas of analysis.

Predvideni študijski rezultati:

Znanje in razumevanje: Obvladanje osnovnih pojmov funkcionalne analize. Sposobnost rekonstrukcije (vsaj lažjih) dokazov.
Sposobnost aplikacije pridobljenega znanja.
Uporaba: Uporaba funkcionalne analize sega tudi v naravoslovje in druga področja znanosti kot na primer ekonomijo.

Refleksija: Razumevanje teorije na podlagi uporabe.

Prenosljive spretnosti – niso vezane le na en predmet: Sposobnost abstraktnega razmišljanja. Spretnost uporabe domače in tuje literature.

Intended learning outcomes:

Knowledge and understanding: Understanding basic concepts of functional analysis. Ability of the reconstruction (at least easier) proofs.
Ability of the application of acquired knowledge.

Application: Functional analysis is used in natural sciences and other areas of science such as economics.

Reflection: Understanding of the theory on the basis of examples.

Transferable skills: Ability to use abstract methods to solve problems. Ability to use a wide range of references and critical thinking.

Metode poučevanja in učenja:

predavanja, vaje, domače naloge, konzultacije

Learning and teaching methods:

Lectures, exercises, homeworks, consultations

Načini ocenjevanja:

Način (pisni izpit, ustno izpraševanje, naloge, projekt):
domače naloge

Delež (v %) /
Weight (in %)

10%
50%

Assessment:

Type (examination, oral, coursework, project):
homeworks

izpit iz vaj	40%	written exam
ustni izpit		oral exam
Ocene: 1-5 (negativno), 6-10 (pozitivno) (po Statutu UL)		Grading: 1-5 (fail), 6-10 (pass) (according to the Statute of UL)

Reference nosilca / Lecturer's references:

Roman Drnovšek:

– DRNOVŠEK, Roman. Common invariant subspaces for collections of operators. Integral equations and operator theory, ISSN 0378-620X, 2001, vol. 39, no. 3, str. 253-266 [COBISS.SI-ID 10597721]

– DRNOVŠEK, Roman. Invariant subspaces for operator semigroups with commutators of rank at most one. Journal of functional analysis, ISSN 0022-1236, 2009, vol. 256, iss. 12, str. 4187-4196 [COBISS.SI-ID 15167321]

– DRNOVŠEK, Roman. An infinite-dimensional generalization of Zenger's lemma. Journal of mathematical analysis and applications, ISSN 0022-247X. [Print ed.], 2012, vol. 388, iss. 2, str. 1233-1238 [COBISS.SI-ID 16214617]

Peter Šemrl:

– ŠEMRL, Peter. Applying projective geometry to transformations on rank one idempotents. Journal of functional analysis, ISSN 0022-1236, 2004, vol. 210, no. , str. 248-257 [COBISS.SI-ID 13012825]

– ŠEMRL, Peter. Similarity preserving linear maps. Journal of operator theory, ISSN 0379-4024, 2008, vol. 60, no. 1, str. 71-83 [COBISS.SI-ID 15079257]

– ŠEMRL, Peter. Symmetries on bounded observables: a unified approach based on adjacency preserving maps. Integral equations and operator theory, ISSN 0378-620X, 2012, vol. 72, iss. 1, str. 7-66 [COBISS.SI-ID 16568665]