

UČNI NAČRT PREDMETA / COURSE SYLLABUS											
Predmet:	Neasociativna algebra										
Course title:	Nonassociative algebra										
Študijski program in stopnja Study programme and level	Študijska smer Study field		Letnik Academic year	Semester Semester							
Magistrski študijski program Matematika	ni smeri		1 ali 2	prvi ali drugi							
Master's study programme Mathematics	none		1 or 2	first or second							
Vrsta predmeta / Course type	izbirni										
Univerzitetna koda predmeta / University course code:	M2222										
Predavanja Lectures	Seminar Seminar	Vaje Tutorial	Klinične vaje work	Druge oblike študija	Samost. delo Individ. work	ECTS					
45		30			105	6					
Nosilec predmeta / Lecturer:	prof. Tomaž Košir										
Jeziki / Languages:	Predavanja / Lectures:	slovenski/Slovene, angleški/English									
	Vaje / Tutorial:	slovenski/Slovene, angleški/English									
Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:	Prerequisites:										
Vsebina:	Content (Syllabus outline):										

Pomembnejši tipi neasociativnih algeber (alternativne algebre, jordanske algebre).	Important types of nonnassociative algebras (alternating algebras, Jordan algebras).
Definicija Liejeve algebre. Ideali in homomorfizmi. Rešljive in nilpotentne Liejeve algebre.	The definition of Lie algebra. Ideals and homomorphisms. Solvable and nilpotent Lie algebras.
Liejev in Cartanov izrek. Killingova forma. Povsem razcepne upodobitve. Upodobitve algeber $sl(2, F)$ . Razcep na korenske podprostore.	Lie's and Cartan's Theorems. The Killing form. Completely irreducible representations. Representations of $sl(2, F)$ . Root subspace decomposition.
Korenski sistemi. Enostavni korenji in Weylova grupa. Klasifikacija (končnorazsežnih) enostavnih Liejevih algeber.	Root systems. Simple roots and the Weyl group. Classification of (finite-dimensional) simple Lie algebras.
Univerzalna ovojna algebra. Poicaré-Birkhoff-Wittov izrek.	Universal enveloping algebra. Theorem Poicaré-Birkhoff-Witt.
Upodobitve enostavnih Liejevih algeber.	Representation theory of simple Lie algebras.

#### **Temeljni literatura in viri / Readings:**

- K. A. Zhevlakov, A. M. Slinko, I. P. Shestakov, A. I. Shirshov, Rings that are nearly associative, Academic Press, 1982.
- J. E. Humphreys: Introduction to Lie Algebras and Representation Theory, Springer, New York-Berlin, 1997.
- J. P. Serre: Complex Semisimple Lie Algebras, Springer, Berlin, 2001.
- W. A. de Graaf: Lie Algebras : Theory and Algorithms, North Holland, Amsterdam, 2000.

#### **Cilji in kompetence:**

Študent spozna osnovne pojme in izreke neasociativne algebre.

#### **Objectives and competences:**

Student meets the fundamental notions and theorems of the nonassociative algebra.

#### **Predvideni študijski rezultati:**

#### **Intended learning outcomes:**

Znanje in razumevanje: Poznavanje osnovnih pojmov in izrekov neasociativne algebre in njihovo prepoznavanje v drugih vejah matematike. Uporaba: V drugih vejah matematike.  Refleksija: Razumevanje teorije na podlagi primerov in uporabe.  Prenosljive spremnosti – niso vezane le na en predmet: Formulacija in reševanje problemov z abstraktnimi metodami.	Knowledge and understanding: Understanding of basic concepts and theorems of noncommutative algebra, and their role in some other areas. Application: In other mathematical areas.  Reflection: Understanding the theory on the basis of examples and applications.  Transferable skills: Formulation and solution of problems using abstract methods.
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Metode poučevanja in učenja:	Learning and teaching methods:
predavanja, vaje, domače naloge, konzultacije	Lectures, exercises, homeworks, consultations

Načini ocenjevanja:	Delež (v %) / Weight (in %)	Assessment:
Način (pisni izpit, ustno izpraševanje, naloge, projekt): izpit iz vaj (2 kolokvija ali pisni izpit)  ustni izpit  Ocene: 1-5 (negativno), 6-10 (pozitivno) (po Statutu UL)	50% 50%	Type (examination, oral, coursework, project): 2 midterm exams instead of written exam, written exam  oral exam  Grading: 1-5 (fail), 6-10 (pass) (according to the Statute of UL)

Reference nosilca / Lecturer's references:
Tomaž Košir:
– GRUNENFELDER, Luzius, GURALNICK, Robert M., KOŠIR, Tomaž, RADJAVI, Heydar. Permutability of characters on algebras. Pacific journal of mathematics, ISSN 0030-8730, 1997, let. 178, št. 1, str.

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- GRUNENFELDER, Luzius, KOŠIR, Tomaž, OMLADIČ, Matjaž, RADJAVI, Heydar. Maximal Jordan algebras of matrices with bounded number of eigenvalues. *Israel journal of mathematics*, ISSN 0021-2172, 2002, vol. 128, str. 53-75 [COBISS.SI-ID 11625305]
- BERNIK, Janez, DRNOVŠEK, Roman, KOKOL-BUKOVŠEK, Damjana, KOŠIR, Tomaž, OMLADIČ, Matjaž, RADJAVI, Heydar. On semitransitive jordan algebras of matrices. *Journal of algebra and its applications*, ISSN 0219-4988, 2011, vol. 10, iss. 2, str. 319-333 [COBISS.SI-ID 15908697]