

UČNI NAČRT PREDMETA / COURSE SYLLABUS							
<b>Predmet:</b>		Uvod v harmonično analizo					
<b>Course title:</b>		Introduction to harmonic analysis					
<b>Študijski program in stopnja</b> Study programme and level		<b>Študijska smer</b> Study field		<b>Letnik</b> Academic year		<b>Semester</b> Semester	
Magistrski študijski program Matematika		ni smeri		1 ali 2		prvi ali drugi	
Master's study programme Mathematics		none		1 or 2		first or second	
<b>Vrsta predmeta / Course type</b>				izbirni			
<b>Univerzitetna koda predmeta / University course code:</b>				M2122			
<b>Predavanja</b> Lectures	<b>Seminar</b> Seminar	<b>Vaje</b> Tutorial	<b>Klinične vaje</b> work	<b>Druge oblike študija</b>	<b>Samost. delo</b> Individ. work	<b>ECTS</b>	
45		30			105	6	
<b>Nosilec predmeta / Lecturer:</b>		doc. Oliver Dragičević					
<b>Jeziki / Languages:</b>		<b>Predavanja / Lectures:</b>		slovenski/Slovene, angleški/English			
		<b>Vaje / Tutorial:</b>		slovenski/Slovene, angleški/English			
<b>Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:</b>				<b>Prerequisites:</b>			
<b>Vsebina:</b>				<b>Content (Syllabus outline):</b>			

<p>Fourierove vrste, sumacijske metode, Riesz-Thorinov interpolacijski izrek,</p> <p>harmonične funkcije, Poissonovi integrali, Hardyjevi prostori, harmonična konjugiranka, Hilbertova transformacija,</p> <p>Schwartzov razred, Fourierova transformacija, distribucije in umirjene distribucije,</p> <p>šibki <math>L_p</math> prostori in Marcinkiewiczev interpolacijski izrek, Paley-Wienerjev izrek ter princip nedoločenosti,</p> <p>Hardy-Littlewoodova maksimalna funkcija,</p> <p>Calderón-Zygmundovi singularni integralni operatorji,</p> <p>linearni parcialni diferencialni operatorji s konstantnimi koeficienti, fundamentalna rešitev, prostori Soboljeva.</p>	<p>Fourier series, summation methods, Riesz-Thorin interpolation theorem,</p> <p>Harmonic functions, Poisson integrals, Hardy spaces, harmonic conjugate, Hilbert transform,</p> <p>Schwartz class, Fourier transform, distributions and tempered distributions,</p> <p>weak <math>L_p</math> spaces and the Marcinkiewicz interpolation theorem, the Paley-Wiener theorem and the uncertainty principle,</p> <p>Hardy-Littlewood maximal function,</p> <p>Calderón-Zygmund singular integral operators,</p> <p>linear partial differential operators with constant coefficients, fundamental solution, Sobolev spaces.</p>
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**Temeljni literatura in viri / Readings:**

L. Grafakos: Classical Fourier Analysis, Second Edition, Graduate Texts in Mathematics 249, Springer, 2008.

E. M. Stein, G. L. Weiss: Introduction to Fourier Analysis on Euclidean Spaces, Princeton University Press, 1971.

A. Torchinsky: Real-Variable Methods in Harmonic Analysis, Academic Press, 1986.

Y. Katznelson: An introduction to harmonic analysis, Dover, New York, 1976.

L. Hörmander: The Analysis of Linear Partial Differential Operators I: Distribution Theory and Fourier Analysis, Berlin Heidelberg New York 1990.

**Cilji in kompetence:**

Spoznavanje temeljnih pojmov in orodij harmonične analize na evklidskih prostorih, umeščanje v kontekst parcialnih diferencialnih enačb.

**Objectives and competences:**

Acquiring knowledge of fundamental notions and tools of euclidean harmonic analysis, placing them into the context of partial differential equations.

**Predvideni študijski rezultati:**

Znanje in razumevanje: Obvladovanje osnovnih konceptov harmonične analize na evklidskih prostorih.

Uporaba: Parcialne diferencialne enačbe, matematična fizika, naravoslovje, medicina.

Refleksija: Gre za eno temeljnih področij sodobne matematične analize.

Prenosljive spretnosti – niso vezane le na en predmet: Prepoznavanje problemov, ki sodijo v področje harmonične analize oziroma formulacija in reševanje nalog s pomočjo metod klasične Fourierove analize.

**Intended learning outcomes:**

Knowledge and understanding: Mastering basic concepts of euclidean harmonic analysis.

Application: PDE, mathematical physics, natural sciences, medicine.

Reflection: The course subject is one of the cornerstones of modern mathematical analysis.

Transferable skills: Recognition of problems in the realm of harmonic analysis, formulation and solving problems with methods of classical Fourier analysis.

**Metode poučevanja in učenja:**

predavanja, vaje, domače naloge, konzultacije

**Learning and teaching methods:**

Lectures, exercises, homeworks, consultations

**Načini ocenjevanja:**

Način (pisni izpit, ustno izpraševanje, naloge, projekt):

domače naloge

ustni zagovor

Ocene: 1-5 (negativno), 6-10 (pozitivno) (po Statutu UL)

Delež (v %) /

Weight (in %)

50%  
50%

**Assessment:**

Type (examination, oral, coursework, project):

homework assignments

oral exam

Grading: 1-5 (fail), 6-10 (pass) (according to the Statute of UL)

**Reference nosilca / Lecturer's references:**

Oliver Dragičević:

- DRAGIČEVIĆ, Oliver. Weighted estimates for powers of the Ahlfors-Beurling operator. Proceedings of the American Mathematical Society, ISSN 0002-9939, 2011, vol. 139, no. 6, str. 2113-2120 [COBISS.SI-ID 15876697]
- DRAGIČEVIĆ, Oliver, VOLBERG, Alexander. Bilinear embedding for real elliptic differential operators in divergence form with potentials. Journal of functional analysis, ISSN 0022-1236, 2011, vol. 261, iss. 10, str. 2816-2828 [COBISS.SI-ID 16051545]
- DRAGIČEVIĆ, Oliver, VOLBERG, Alexander. Linear dimension-free estimates in the embedding theorem for Schrödinger operators. Journal of the London Mathematical Society, ISSN 0024-6107, 2012, vol. 85, p. 1, str. 191-222 [COBISS.SI-ID 16214873]