

UČNI NAČRT PREDMETA / COURSE SYLLABUS											
Predmet:	Uvod v geometrijsko topologijo										
Course title:	Introduction to geometric topology										
Študijski program in stopnja Study programme and level	Študijska smer Study field		Letnik Academic year	Semester Semester							
Enoviti magistrski študijski program Pedagoška matematika	ni smeri		3 ali 4	drugi							
Integrated Master's study programme Pedagogical Mathematics	none		3 or 4	second							
Vrsta predmeta / Course type	izbirni										
Univerzitetna koda predmeta / University course code:	M0537										
Predavanja Lectures	Seminar Seminar	Vaje Tutorial	Klinične vaje work	Druge oblike študija	Samost. delo Individ. work	ECTS					
30		30			90	5					
Nosilec predmeta / Lecturer:	prof. Dušan Repovš, prof. Sašo Strle										
Jeziki / Languages:	Predavanja / Lectures:	slovenski/Slovene									
	Vaje / Tutorial:	slovenski/Slovene									
Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:	Prerequisites:										
Opravljen predmet Splošna topologija.	Completed course Point-set topology.										
Vsebina:	Content (Syllabus outline):										

Kvocientna topologija, zvezne preslikave na kvocientih, zlepki. Delovanja grup in prostori orbit. Projektivni prostori.	Quotient topology, continuous maps on quotients, adjunction spaces. Group actions and orbit spaces. Projective spaces.
Brouwerjev izrek o negibni točki, Jordanov izrek, Brouwerjev izrek o invarianci odprtih množic.	Brouwer's fixed point theorem, the Jordan curve theorem, Brouwer's invariance of domain theorem.
Topološke mnogoterosti, konstrukcije mnogoterosti. Poliedrske ploskve, Eulerjeva karakteristika. Klasifikacija sklenjenih ploskev.	Topological manifolds constructions of manifolds. Polyhedral surfaces, Euler characteristic. Classification of closed surfaces.
Simplicialni kompleksi in poliedri.	Simplicial complexes and polyhedra.

#### **Temeljni literatura in viri / Readings:**

J. Dugundji: Topology, Allyn and Bacon, Boston, 1978.

W. S. Massey: Algebraic Topology: An Introduction, Springer, New York-Heidelberg, 1989.

J. R. Munkres: Topology : A First Course, Prentice Hall, Englewood Cliffs, 1975.

#### **Cilji in kompetence:**

Študent spozna osnovne pojme topologije evklidskih prostorov in geometrijske topologije kot so Jordanov in Brouwerjev izrek, simplicialni kompleksi in poliedri ter mnogoterosti.

#### **Objectives and competences:**

Student gets familiar with basic concepts of topology of Euclidian spaces and geometric topology, such as Jordan and Brouwer theorems, simplicial complexes and polyhedra and manifolds.

#### **Predvideni študijski rezultati:**

Znanje in razumevanje: Razumevanje pojmov kvocientne topologije, osnovnih vprašanj topologije evklidskih prostorov ter odnosa med lokalno in globalno podobo geometrijskih objektov. Poznavanje osnovnih prijemov za delo z geometričnimi objekti.

#### **Intended learning outcomes:**

Knowledge and understanding: Understanding of notions such as quotient topology, basic questions of topology of Euclidian spaces and relations between local and global picture of geometric objects. Knowledge of basic concepts of geometric objects.

<p><b>Uporaba:</b> V področjih matematike, ki delajo z geometričnimi objekti (kompleksna in globalna analiza, dinamični sistemi, numerična matematika, mehanika, teorija grafov), v računalništvu (grafika, prepoznavanje vzorcev), v fiziki, kemiji in drugih naravoslovnih in tehničnih vedah.</p> <p><b>Refleksija:</b> Razumevanje teorije na podlagi primerov in uporabe.</p> <p><b>Prenosljive spretnosti – niso vezane le na en predmet:</b> Formulacija problemov v primernem jeziku, reševanje in analiza doseženega na primerih, prehajanje iz lokalnih na globalne lastnosti.</p>	<p><b>Application:</b> In the fields of mathematics, where geometric objects do appear (complex and global analysis, dynamic systems, numerical mathematics, mechanics, graph theory), in computing (graphics, pattern recognition), in physics, chemistry and other natural sciences and engineering.</p> <p><b>Reflection:</b> Understanding of the theory from the applications.</p> <p><b>Transferable skills:</b> Formulation of the problem in an appropriate language, the ability to solve and analyze the progress on the cases, the transition from local to global properties.</p>
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#### **Metode poučevanja in učenja:**

Predavanja, vaje, domače naloge, seminarske naloge, konzultacije

#### **Learning and teaching methods:**

Lectures, exercises, homework, seminar work, consultations

#### **Načini ocenjevanja:**

Način (pisni izpit, ustno izpraševanje, naloge, projekt):  
izpit iz vaj,  
izpit iz teorije  
ocene: 1-5 (negativno), 6-10 (pozitivno) (po Statutu UL)

Delež (v %) /

Weight (in %)

50%  
50%

#### **Assessment:**

Type (examination, oral, coursework, project):  
written exam  
  
oral exam  
  
grading: 1-5 (fail), 6-10 (pass) (according to the Statute of UL)

#### **Reference nosilca / Lecturer's references:**

Dušan Repovš:

- BANAKH, Taras, REPOVŠ, Dušan. Direct limit topologies in the categories of topological groups and of uniform spaces. *Tohoku mathematical journal*, ISSN 0040-8735, 2012, vol. 64, no. 1, str. 1-24 [COBISS.SI-ID 16215897]
- CÁRDENAS, Manuel, LASHERAS, Francisco F., QUINTERO, Antonio, REPOVŠ, Dušan. On manifolds with nonhomogeneous factors. *Central European Journal of Mathematics*, ISSN 1895-1074, 2012, vol. 10, no. 3, str. 857-862 [COBISS.SI-ID 16241753]
- KARIMOV, Umed H., REPOVŠ, Dušan. On generalized 3-manifolds which are not homologically locally connected. *Topology and its Applications*, ISSN 0166-8641. [Print ed.], 2013, vol. 160, iss. 3, str. 445-449 [COBISS.SI-ID 16558681]
- CENCELJ, Matija, REPOVŠ, Dušan. *Topologija*, (Zbirka Pitagora). 1. ponatis. Ljubljana: Pedagoška fakulteta, 2011. XVI, 169 str., ilustr. ISBN 978-86-7735-051-2 [COBISS.SI-ID 254230528]

Sašo Strle:

- OWENS, Brendan, STRLE, Sašo. A characterisation of the  $n < 1>[oplus] < 3>$  form and applications to rational homology spheres. *Mathematical research letters*, ISSN 1073-2780, 2006, vol. 13, iss. 2, str. 259-271 [COBISS.SI-ID 13873241]
- GRIGSBY, J. Elisenda, RUBERMAN, Daniel, STRLE, Sašo. Knot concordance and Heegaard Floer homology invariants in branched covers. *Geometry & topology*, ISSN 1364-0380, 2008, vol. 12, iss. 4, str. 2249-2275 [COBISS.SI-ID 14892121]
- OWENS, Brendan, STRLE, Sašo. A characterization of the  $Z^{[sup] n} [oplus] Z^{([\delta])}$  lattice and definite nonunimodular intersection forms. *American journal of mathematics*, ISSN 0002-9327, 2012, vol. 134, no. 4, str. 891-913 [COBISS.SI-ID 16408153]