

UČNI NAČRT PREDMETA / COURSE SYLLABUS (leto / year 2017/18)									
Predmet:	Algebraične krivulje								
Course title:	Algebraic curves								
Študijski program in stopnja Study programme and level	Študijska smer Study field		Letnik Academic year	Semester Semester					
Univerzitetni študijski program Finančna matematika	ni smeri		3	drugi					
First cycle academic study programme Financial Mathematics	none		3	second					
Vrsta predmeta / Course type	izbirni / elective								
Univerzitetna koda predmeta / University course code:	M0343								
Predavanja Lectures	Seminar Seminar	Vaje Tutorial	Klinične vaje work	Druge oblike študija	Samost. delo Individ. work	ECTS			
30		30			90	5			
Nosilec predmeta / Lecturer:	prof. dr. Tomaž Košir, prof. dr. Pavle Saksida								
Jeziki / Languages:	Predavanja / slovenski / Slovene Lectures: Vaje / Tutorial: slovenski / Slovene								
Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:	Prerequisites:								
Vpis v letnik študija.  Opravljen predmet Algebra 1.	Enrolment in the programme.  Completed course Algebra 1.								
Vsebina:	Content (Syllabus outline):								

Afine algebraične krivulje. Nerazcepnot in povezanost.	Affine algebraic curves. Irreducibility and connectedness.
Projektivno zaprtje. Presečna večkratnost med krivuljo in premico. Bezouteva lema.	Projectivization. Multiplicity of intersection between a line and a curve. Bezout lemma.
Tangente. Singularnosti.	Tangents. Singularity.
Polare in Hessove krivulje.	Polars and Hess curves.
Dualna krivulja. Plückerjeva formula.	Dual curve. Plücker formula.
Racionalne krivulje. Stožnice.	Rational curves , Conics.
Kubične krivulje.	Cubic curves.
Izrek o rodu in stopnji nesingularne krivulje.	Degree-genus formula for nonsingular curves.

#### **Temeljni literatura in viri / Readings:**

- G. Fisher: Plane Algebraic Curves, AMS, Providence, 2001.
- C. G. Gibson: Elementary Geometry of Algebraic Curves, Cambridge Univ. Press, Cambridge, 1998.
- M. Reid: Undergraduate Algebraic Geometry, Cambridge Univ. Press, Cambridge, 1988.
- K. Hulek: Elementary Algebraic Geometry, AMS, Providence, 2003.
- F. Kirwan: Complex Algebraic Curves, Cambridge Univ. Press, Cambridge, 1992.
- C. H. Clemens: A Scrapbook of Complex Curve Theory, 2nd edition, AMS, Providence, 2003.

#### **Cilji in kompetence:**

Je eden od treh osnovnih predmetov, pri katerem študent spozna geometrijski način razmišljanja. Osnovni cilj je spoznati temeljne pojme in lastnosti algebraičnih krivulj.

#### **Objectives and competences:**

This is one of the three basic courses in which students learn to think geometrically. The basic goal is to understand the basic definitions and properties of algebraic curves.

#### **Predvideni študijski rezultati:**

Znanje in razumevanje: Razumevanje povezave med algebraičnimi enačbami in geometrijskimi objekti. Sposobnost obravnave geometrijskih

#### **Intended learning outcomes:**

Knowledge and understanding: Understanding the relation between the algebraic equations and the geometric objects. Ability of treating

objektov s pomočjo orodij iz teorije polinomov. Poznavanje in razumevanje osnovnih pojmov in definicij iz teorije algebraičnih krivulj in algebraične geometrije.

Uporaba: Algebraični opis objektov, ki se pojavljajo pri problemih v drugih vejah matematike in njene uporabe. Uporaba algebraično-geometrijskih sredstev pri obravnavi teh problemov.

Refleksija: Dojemanje istih objektov (krivulj) z različnih aspektov. Razvijanje geometrijskega razmišljanja pri reševanju problemov iz prakse.

Prenosljive spremnosti – niso vezane le na en predmet: Formulacija problemov v primernem jeziku, reševanje in analiza doseženega na primerih. Ker je za razumevanje predmeta potrebno solidno obvladanje nekaterih vsebin iz analize in linearne algebре, se študent nauči uporabljati znanje, pridobljeno pri drugih predmetih. Nauči se tudi spremnosti uporabe tuje literature.

some geometric problems by means of tools, coming from the theory of polynomials. Knowledge and understanding of the fundamental concepts of the theory of algebraic curves and algebraic geometry.

Application: Algebraic description of objects, appearing in problems from other areas of mathematics and its applications. Application of algebro-geometric methods in the treatment of such problems.

Reflection: Ability of percieving mathematical object from different points of view. Development of the geometric approach to solving problems in applicative mathematics.

Transferable skills: Formulation of problems in suitable contexts, evaluation of developed tools in concrete examples. This course demands a firm knowledge of certain chapters from mathematical analysis and algebra. Therefore students learn how to use previously acquired knowledge in new situations. Students learn the use of study literature in foreign languages.

#### Metode poučevanja in učenja:

Predavanja, vaje, konzultacije

#### Learning and teaching methods:

Lectures, exercises, consultations

#### Načini ocenjevanja:

Delež (v %) /

Weight (in %)

#### Assessment:

Način (pisni izpit, ustno izpraševanje, naloge, projekt):

50%  
50%

Type (examination, oral, coursework, project):

2 kolokvija namesto izpita iz vaj, izpit iz vaj,

2 midterm exams instead of written exam, written exam

izpit iz teorije  ocene: 1-5 (negativno), 6-10 (pozitivno) (po Statutu UL)		oral exam  grading: 1-5 (fail), 6-10 (pass) (according to the Statute of UL)
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**Reference nosilca / Lecturer's references:**

- GRUNENFELDER, Luzius, GURALNICK, Robert M., KOŠIR, Tomaž, RADJAVI, Heydar. Permutability of characters on algebras. *Pacific journal of mathematics*, ISSN 0030-8730, 1997, let. 178, št. 1, str. 63-70. [COBISS.SI-ID 7437145]
- GRUNENFELDER, Luzius, KOŠIR, Tomaž. Coalgebras and spectral theory in one and several parameters. V: GOHBERG, I. (ur.), LANCASTER, P. (ur.), SHIVAKUMAR, P. N. (ur.). Recent developments in operator theory and its applications : International Conference in Winnipeg, October 2-6, 1994, (Operator theory, ISSN 0255-0156, vol. 87). Basel, Boston, Berlin: Birkhäuser, cop. 1996, str. 177-192. [COBISS.SI-ID 7436889]
- GRUNENFELDER, Luzius, KOŠIR, Tomaž. Koszul cohomology for finite families of comodule maps end applications. *Communications in algebra*, ISSN 0092-7872, 1997, let. 25, št. 2, str. 459-479. [COBISS.SI-ID 7127641]
- SAKSIDA, Pavle. Nahm's equations and generalizations Neumann system. *Proceedings of the London Mathematical Society*, ISSN 0024-6115, 1999, let. 78, št. 3, str. 701-720. [COBISS.SI-ID 8853849]
- SAKSIDA, Pavle. Neumann system, spherical pendulum and magnetic fields. *Journal of physics. A, Mathematical and general*, ISSN 0305-4470, 2002, vol. 35, no. 25, str. 5237-5253. [COBISS.SI-ID 11920217]
- SAKSIDA, Pavle. Integrable anharmonic oscillators on spheres and hyperbolic spaces. *Nonlinearity*, ISSN 0951-7715, 2001, vol. 14, no. 5, str. 977-994. [COBISS.SI-ID 10942809]