

| UČNI NAČRT PREDMETA / COURSE SYLLABUS (leto / year 2016/17)                  |                           |   |                              |                                    |                                      |                             |
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| <b>Predmet:</b>  |                           | Nekomutativna algebra   |                              |                                    |                                      |                             |
| <b>Course title:</b>   |                           | Noncommutative algebra  |                              |                                    |                                      |                             |
| <b>Študijski program in stopnja</b><br>Study programme and level             |                           | <b>Študijska smer</b><br>Study field                                  |                              | <b>Letnik</b><br>Academic year     |                                      | <b>Semester</b><br>Semester |
| Magistrski študijski program<br>Finančna matematika                          |                           | ni smeri  |                              | 1 ali 2                            |                                      | prvi ali drugi              |
| Master's study programme<br>Financial Mathematics                            |                           | none  |                              | 1 or 2                             |                                      | first or second             |
| <b>Vrsta predmeta / Course type</b>  |                           |   |                              | izbirni / elective                 |                                      |                             |
| <b>Univerzitetna koda predmeta / University course code:</b>                 |                           |   |                              | M2211                              |                                      |                             |
| <b>Predavanja</b><br>Lectures  | <b>Seminar</b><br>Seminar | <b>Vaje</b><br>Tutorial   | <b>Klinične vaje</b><br>work | <b>Druge oblike</b><br>študija     | <b>Samost. delo</b><br>Individ. work | <b>ECTS</b>                 |
| 45   |                           | 30  |                              |                                    | 105                                  | 6                           |
| <b>Nosilec predmeta / Lecturer:</b>  |                           | prof. dr. Matej Brešar, prof. dr. Jakob Cimprič                       |                              |                                    |                                      |                             |
| <b>Jeziki / Languages:</b>   |                           | <b>Predavanja / Lectures:</b> slovenski / Slovene, angleški / English |                              |                                    |                                      |                             |
|  |                           | <b>Vaje / Tutorial:</b> slovenski / Slovene, angleški / English       |                              |                                    |                                      |                             |
| <b>Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:</b> |                           |   |                              | <b>Prerequisites:</b>              |                                      |                             |
| Vpis v letnik študija.   |                           |   |                              | Enrolment in the programme.        |                                      |                             |
| <b>Vsebina:</b>  |                           |   |                              | <b>Content (Syllabus outline):</b> |                                      |                             |

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| <p>Nekomutativni obsegi. Frobeniusov izrek. Wedderburnov izrek o končnih obsekih.</p> <p>Radikal. Polenostavne algebre. Wedderburnov izrek. Maschkejev izrek.</p> <p>Enostavni in polenostavni moduli. Izrek o gostoti. Jacobsonov radikal.</p> <p>Tenzorski produkti algeber. Skolem-Noetherin izrek. Izrek o drugem centralizatorju. Brauerjeva grupa.</p> | <p>Noncommutative division rings. Frobenius' theorem. Wedderburn's theorem on finite division rings.</p> <p>Radical. Semisimple algebras. Wedderburn's theorem. Maschke's theorem.</p> <p>Simple and semisimple modules. Density theorem. Jacobson radical.</p> <p>Tensor product of algebras. Skolem-Noether theorem. Double centralizer theorem. Brauer group.</p> |
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### Temeljni literatura in viri / Readings:

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| <p>R. K. Dennis, B. Farb, Noncommutative algebra, Springer, 1993.</p> <p>T. Y. Lam, A first course in noncommutative rings, Springer, 2001.</p> <p>R. S. Pierce, Associative algebras, Springer, 1982.</p> <p>L. Rowen, Graduate algebra: Noncommutative view, AMS, 2008.</p> <p>M. Brešar, Introduction to Noncommutative Algebra, Springer, 2014</p> |
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### Cilji in kompetence:

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| <p>Spoznati osnovne pojme in orodja nekomutativne algebre.</p> |
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### Objectives and competences:

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| <p>To master basic concepts and tools of noncommutative algebra.</p> |
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### Predvideni študijski rezultati:

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| <p>Znanje in razumevanje:</p> <p>Razumevanje osnovnih pojmov in izrekov nekomutativne algebre ter njihove vloge na nekaterih drugih področjih.</p> <p>Uporaba:</p> <p>V drugih vejah matematike.</p> |
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### Intended learning outcomes:

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| <p>Knowledge and understanding:</p> <p>Understanding of basic concepts and theorems of noncommutative algebra, and their role in some other areas.</p> <p>Application:</p> <p>In other mathematical areas.</p> |
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| <p><b>Refleksija:</b></p> <p>Razumevanje teorije na podlagi primerov in uporabe.</p> <p>Prenosljive spretnosti – niso vezane le na en predmet:</p> <p>Formulacija in reševanje problemov z abstraktnimi metodami.</p> | <p><b>Reflection:</b></p> <p>Understanding the theory on the basis of examples and applications.</p> <p>Transferable skills:</p> <p>Formulation and solution of problems using abstract methods.</p> |
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| <p><b>Metode poučevanja in učenja:</b></p> <p>Predavanja, vaje, domače naloge, konzultacije.</p> | <p><b>Learning and teaching methods:</b></p> <p>Lectures, exercises, homeworks, consultations.</p> |
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| <b>Načini ocenjevanja:</b>                                | Delež (v %) /<br>Weight (in %) | <b>Assessment:</b>  |
|---|--------------------------------|---|
| Način (pisni izpit, ustno izpraševanje, naloge, projekt): |                                | Type (examination, oral, coursework, project):                    |
| domače naloge   |                                | homework assignment   |
| ustni izpit   | 50%                            | oral exam   |
| Ocene: 1-5 (negativno), 6-10 (pozitivno) (po Statutu UL)  | 50%                            | Grading: 1-5 (fail), 6-10 (pass) (according to the Statute of UL) |

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| <p><b>Reference nosilca / Lecturer's references:</b></p> <p>Matej Brešar:</p> <p>BREŠAR, Matej, CHEBOTAR, M. A., MARTINDALE, Wallace S. Functional identities, (Frontiers in mathematics). Basel, Boston, Berlin: Birkhäuser, cop. 2007. XII, 272 str. ISBN 978-3-7643-7795-3. ISBN 978-3-7643-7796-0. [COBISS.SI-ID 14332505]</p> <p>BREŠAR, Matej. An elementary approach to Wedderburn's structure theory. Expositiones mathematicae, ISSN 0723-0869, 2010, vol. 28, no 1, str. 79-83. [COBISS.SI-ID 15382617]</p> |
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BREŠAR, Matej. An alternative approach to the structure theory of PI-rings. *Expositiones mathematicae*, ISSN 0723-0869, 2011, vol. 29, no 1, str. 159-164. [COBISS.SI-ID 15859545]

Jaka Cimprič:

CIMPRIČ, Jaka. Free skew fields have many [ast]-orderings. *Journal of algebra*, ISSN 0021-8693, 2004, vol. 280, no. 1, str. 20-28. [COBISS.SI-ID 13210201]

CIMPRIČ, Jaka. Formally real involutions on central simple algebras. *Communications in algebra*, ISSN 0092-7872, 2008, vol. 36, no. 1, str. 165-178. [COBISS.SI-ID 14613337]

CIMPRIČ, Jaka, HELTON, J. William, MCCULLOUGH, Scott, NELSON, Christopher. A noncommutative real nullstellensatz corresponds to a noncommutative real ideal: algorithms. *Proceedings of the London Mathematical Society*, ISSN 0024-6115, 2013, vol. 106, iss. 5, str. 1060-1086. [COBISS.SI-ID 16636249]