

UČNI NAČRT PREDMETA / COURSE SYLLABUS (leto / year 2017/18)									
Predmet:	Teorija grafov								
Course title:	Graph theory								
Študijski program in stopnja Study programme and level	Študijska smer Study field		Letnik Academic year	Semester Semester					
Magistrski študijski program Finančna matematika	ni smeri		1 ali 2	prvi ali drugi					
Master's study programme Financial Mathematics	none		1 or 2	first or second					
Vrsta predmeta / Course type	izbirni / elective								
Univerzitetna koda predmeta / University course code:	M2213								
Predavanja Lectures	Seminar Seminar	Vaje Tutorial	Klinične vaje work	Druge oblike študija	Samost. delo Individ. work	ECTS			
45		30			105	6			
Nosilec predmeta / Lecturer:	prof. dr. Sandi Klavžar, prof. dr. Primož Potočnik, prof. dr. Riste Škrekovski, prof. dr. Arjana Žitnik								
Jeziki / Languages:	Predavanja / Lectures: slovenski / Slovene, angleški / English Vaje / Tutorial: slovenski / Slovene, angleški / English								
Pogoji za vključitev v delo oz. za opravljanje študijskih obveznosti:	Prerequisites:								
Vpis v letnik študija.	Enrolment in the programme.								
Vsebina:	Content (Syllabus outline):								

Prirejanja in faktorji (min-max izreki, neodvisne množice in pokritja, Tutov izrek o 1-faktorju)	Matchings and factors (min-max theorem, independent sets and coverings, Tutte's 1-factor theorem)
Povezanost (struktura 2-povezanih in k-povezanih grafov, dokaz in uporabe Mengerjevih izrekov)	Graph connectivity (structure of 2-connected and k-connected graphs, Menger theorem and its applications)
Barvanja grafov (meje, dokaz Brooksovega izreka, struktura k-kromatičnih grafov, Turanov izrek, kromatični polinom, tetivni grafi)	Graph colorings (bounds of the chromatic number, structure of k-chromatic graphs, Turan's theorem, chromatical polynomial, chordal graphs)
Ravninski grafi (dualni graf, izrek Kuratowskega, konveksne vložitve, barvanja ravninskih grafov, prekrižno število)	Planar graphs (dual graph, Kuratowski's theorem, convex embedding, colorings of planar graphs, crossing number)
Predavatelj izbere še eno izmed naslednjih tem: barvanja povezav in graf povezav, hamiltonski grafi, popolni grafi, ekstremalni problemi, dominacija v grafih, simetrijske lastnosti grafov II.	Instructor chooses an addition topic from the following list: edge colorings and line graphs, Hamiltonian graphs, perfect graphs, extremal graph problems, graph domination, symmetry properties of graphs II.

#### **Temeljni literatura in viri / Readings:**

- R. Diestel: Graph Theory, 3. izdaja, Springer, Berlin, 2005.  
A. Bondy, U.S.R. Murty: Graph Theory, 2. izdaja, Springer, Berlin, 2008.  
D. West: Introduction to Graph Theory, 2. izdaja, Prentice Hall, Upper Saddle River, 2005.  
R. J. Wilson, M. Watkins: Uvod v teorijo grafov, DMFA Slovenije, Ljubljana, 1997.

#### **Cilji in kompetence:**

Študent poglobi in razširi znanje teorije grafov. Spozna uporabnost grafov in omrežij na različnih področjih matematike ter možnosti za njihovo uporabo tudi v drugih vejah znanosti.

#### **Objectives and competences:**

Students will deepen and broaden their knowledge of graph theory, and learn about the usefulness of graphs and networks in different areas of mathematics and their potential use in other branches of science.

#### **Predvideni študijski rezultati:**

#### **Intended learning outcomes:**

<p>Znanje in razumevanje: Slušatelj poglobi znanje iz teorije grafov.</p> <p>Uporaba: Grafi omogočajo matematično modeliranje različnih pojavov. Slušatelj se seznani z vrsto matematičnih rezultatov, ki opisujejo lastnosti grafov in tako omogočajo matematično analizo modelov, opisanih z grafi.</p> <p>Refleksija: Povezovanje teoretičnih spoznanj s praktičnimi uporabami na primer v optimizaciji in pri programiranju. Sposobnost prepoznavanja problemov, ki jih lahko uspešno opišemo z grafi.</p> <p>Prenosljive spremnosti – niso vezane le na en predmet: Sposobnost opisa problemov iz vsakdanjega življenja s pomočjo matematičnih struktur, še posebej z grafi. Sposobnost uporabe matematičnih orodij za reševanje problemov.</p>	<p><b>Knowledge and understanding:</b> Students deepen their knowledge of graph theory.</p> <p><b>Application:</b> Graphs allow mathematical modeling of variety of phenomena. Students learn various mathematical results that describe properties of graphs and thus provide a mathematical analysis of the models described by graphs.</p> <p><b>Reflection:</b> Integration of theoretical knowledge with practical applications such as optimization and programming. Ability to recognize problems that can be successfully described by graphs.</p> <p><b>Transferable skills:</b> The ability to describe practical problems with the help of mathematical structures, in particular with graphs. The ability to use mathematical tools to solve problems.</p>
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#### Metode poučevanja in učenja:

predavanja, vaje, domače naloge, konzultacije

#### Learning and teaching methods:

lectures, exercises, homeworks, consultations

#### Načini ocenjevanja:

Delež (v %) /

Weight (in %)

#### Assessment:

<p>Način (pisni izpit, ustno izpraševanje, naloge, projekt):</p> <p>izpit iz vaj (pisni izpit)</p> <p>ustni izpit</p> <p>Ocene: 1-5 (negativno), 6-10 (pozitivno) (po Statutu UL)</p>	<p>50%</p> <p>50%</p> <p></p> <p></p>	<p>Type (examination, oral, coursework, project):</p> <p>written exam</p> <p>oral exam</p> <p>Grading: 1-5 (fail), 6-10 (pass) (according to the Statute of UL)</p>
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**Reference nosilca / Lecturer's references:**

Primož Potočnik:

POTOČNIK, Primož. Tetravalent arc-transitive locally-Klein graphs with long consistent cycles. European journal of combinatorics, ISSN 0195-6698, 2014, vol. 36, str. 270-281. [COBISS.SI-ID 16862041]

POTOČNIK, Primož, SPIGA, Pablo, VERRET, Gabriel. Cubic vertex-transitive graphs on up to 1280 vertices. Journal of symbolic computation, ISSN 0747-7171, 2013, vol. 50, str. 465-477. [COBISS.SI-ID 16520537]

POTOČNIK, Primož. Edge-colourings of cubic graphs admitting a solvable vertex-transitive group of automorphisms. Journal of combinatorial theory. Series B, ISSN 0095-8956, 2004, vol. 91, no. 2, str. 289-300. [COBISS.SI-ID 13087321]

Sandi Klavžar:

KLAVŽAR, Sandi, SHPECTOROV, Sergey. Convex excess in partial cubes. Journal of graph theory, ISSN 0364-9024, 2012, vol. 69, no. 4, str. 356-369. [COBISS.SI-ID 16243033]

BREŠAR, Boštjan, KLAVŽAR, Sandi, RALL, Douglas. Domination game and an imagination strategy. SIAM journal on discrete mathematics, ISSN 0895-4801, 2010, vol. 24, no. 3, str. 979-991. [COBISS.SI-ID 15648089]

KLAVŽAR, Sandi. On the canonical metric representation, average distance, and partial Hamming graphs. European journal of combinatorics, ISSN 0195-6698, 2006, vol. 27, no. 1, str. 68-73. [COBISS.SI-ID 13858905]

Riste Škrekovski:

GOVORČIN, Jelena, KNOR, Martin, ŠKREKOVSKI, Riste. Line graph operation and small worlds. Information processing letters, ISSN 0020-0190. [Print ed.], 2013, vol. 113, iss. 5-6, str. 196-200. [COBISS.SI-ID 16561497]

DVOŘÁK, Zdeněk, LIDICKÝ, Bernard, ŠKREKOVSKI, Riste. Randić index and the diameter of a graph. European journal of combinatorics, ISSN 0195-6698, 2011, vol. 32, iss. 3, str. 434-442. [COBISS.SI-ID 17410905]

KAISET, Tomáš, STEHLÍK, Matěj, ŠKREKOVSKI, Riste. On the 2-resonance of fullerenes. SIAM journal on discrete mathematics, ISSN 0895-4801, 2011, vol. 25, no. 4, str. 1737-1745. [COBISS.SI-ID 16244569]

Arjana Žitnik:

MILANIČ, Martin, PISANSKI, Tomaž, ŽITNIK, Arjana. Dilation coefficient, plane-width, and resolution coefficient of graphs. *Monatshefte für Mathematik*, ISSN 0026-9255, 2013, vol. 170, no. 2, str. 179-193. [COBISS.SI-ID 1024499540]

ŽITNIK, Arjana, HORVAT, Boris, PISANSKI, Tomaž. All generalized Petersen graphs are unit-distance graphs. *Journal of the Korean Mathematical Society*, ISSN 0304-9914, 2012, vol. 49, no. 3, str. 475-491. [COBISS.SI-ID 16217945]

JURIŠIĆ, Aleksandar, TERWILLIGER, Paul, ŽITNIK, Arjana. The Q-polynomial idempotents of a distance-regular graph. *Journal of combinatorial theory. Series B*, ISSN 0095-8956, 2010, vol. 100, iss. 6, str. 683-690. [COBISS.SI-ID 15688537]